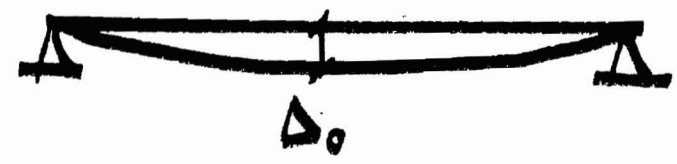
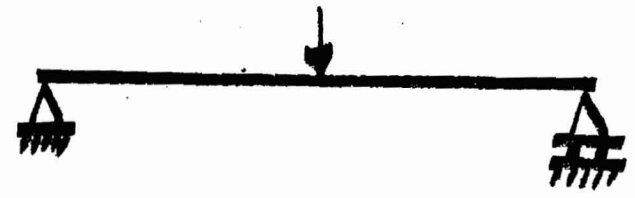
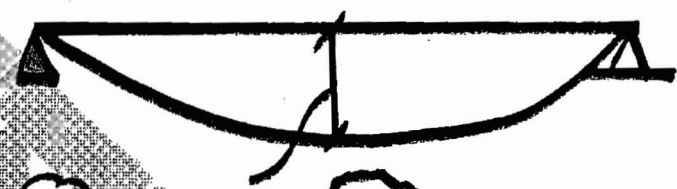


# Creep in Bending

# الزحف من الإحناء



بعد التحميل



بعد زمن

الزحف بعد زمن (t)  $y = \Delta_0 + \Delta_c$

دس بكام /  $\Delta_c$

• يحدث زحف [تدعيم] للتكررات مثل ما يحدث من الأجسام المعرضة لنتيجة عامل الوقت .

وبالمثل تتغير الأبعاد وتُحسب من

لعلاقة :

$$P_{cr} = P_e \cdot \left( \frac{2n+1}{3n} \right)$$

ممكن استبدال الثابت  $(K_4 \leftarrow n)$  للزحف  $\Delta_c$  كالتالي

والزحف من العلاقة :

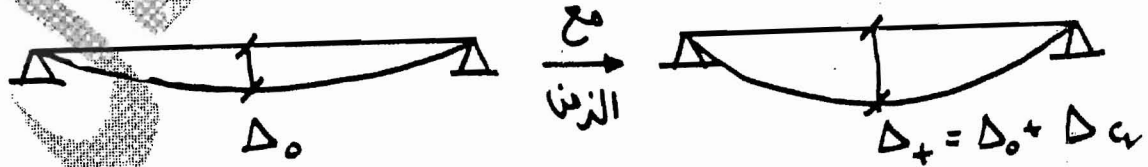
$$\frac{\partial^2 y}{\partial x^2} = \frac{t}{A} M_x^n$$

(1)

- : t : time
- : A : Const
- : n = Const =  $K_4$

# Creep in Bending

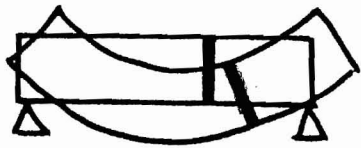
\* يحدث زحف للكمرات فيزداد الهبوط الناتج .



→ للحكم على الزحف في الإنشاء سيتم فرض مجموعة فروض :

→ Assumption for mechanism of creep in Bending :

١. إهمال القصر الناتج من الإنشاء .



٢. المستويات تظل مستويات بعد التحميل .

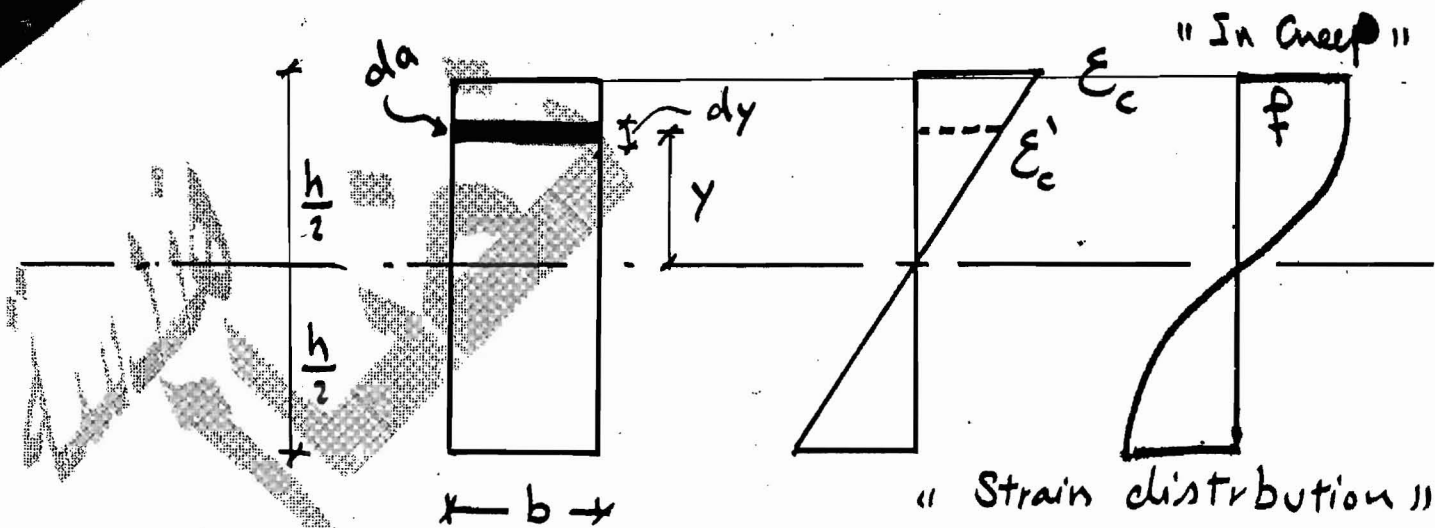
٣. لعلاقة مستتجة بين الزحف والإجهاد و الزمن

من الشد هو نفسها من الضغط .

٤. عند أي قطاع من الكمر القوة الموصولة متكافئة

[ تلوين = صفراء ]

٥. العزوم الناتجة من الأحمال الخارجية = لعزوم ناتجة من الإجهادات الداخلية



$$\therefore \frac{\epsilon'_c}{\epsilon_c} = \frac{y}{(h/2)} \rightarrow \textcircled{1}$$

← من تشابه المثلثات :

$$\therefore \left( \epsilon = B \cdot f^n \cdot t \right)$$

$$\therefore \epsilon'_c = B t \frac{f_c^n}{\epsilon_c} \quad \& \quad \epsilon_c = B t \frac{f_c^n}{\epsilon_c}$$

$$\frac{B t \frac{f_c^n}{\epsilon_c}}{B t \frac{f_c^n}{\epsilon_c}} = \frac{y}{(h/2)}$$

بالتعويض في (1) :

$$\therefore f'_c = \left( \frac{y}{h/2} \right)^{1/n} \cdot f_c$$

ممكن

$$M = \int_{-h/2}^{+h/2} f'_c \cdot da \cdot y$$

$$= \int_{-h/2}^{+h/2} f_c \cdot \left( \frac{y}{h/2} \right)^{1/n} \cdot b \cdot dy \cdot y$$

$$= \int_{-h/2}^{+h/2} \frac{f_c \cdot b}{\left( \frac{h}{2} \right)^{1/n}} \cdot y \cdot y^{1/n} \cdot dy$$

نرمز = قوة مساهمة  
إجهاد مساهمة

$$da = b \cdot dy$$

$$\therefore M = \int_{-h/2}^{+h/2} \frac{f_c \cdot b}{(h/2)^{1/n}} \cdot y \cdot y^{1/n} \cdot dy$$

$$= \frac{f_c \cdot b}{(h/2)^{1/n}} \cdot \int_{-h/2}^{+h/2} y^{(1+\frac{1}{n})} \cdot dy$$

$$= \frac{f_c \cdot b}{[h/2]^{1/n}} \cdot \left[ \frac{y^{2+\frac{1}{n}}}{2+\frac{1}{n}} \right]_{-\frac{h}{2}}^{h/2}$$

$$\therefore M = \frac{f_c \cdot b}{(h/2)^{1/n} \cdot (2+\frac{1}{n})} \cdot (2) \cdot \left[ h/2 \right]^{2+\frac{1}{n}}$$

$$\therefore f_c = \frac{M \cdot (h/2)^{1/n} \cdot (2+\frac{1}{n})}{2 \cdot b \cdot (h/2)^{2+\frac{1}{n}}}$$

$$\therefore f_c = \frac{M \cdot h}{I \cdot 2} \left( \frac{2n+1}{3n} \right)$$

والافتتاح  
 $\left( \frac{h/6}{h/6} \right)$

$$\therefore I = \frac{bh^3}{12}$$

$$\therefore f_c = f_{\text{elastic}} \cdot \left( \frac{2n+1}{3n} \right)$$

$$f_{\text{elastic}} = \frac{M}{I} \cdot \frac{h}{2}$$

$$\therefore \underline{n \geq 1}$$

$n=1$  في صورة  $k$

# \* Creep Deflection :

الزحف الناتج  
من الزحف

from shape:  $\Delta CC'm$  &  $\Delta Kmo$

$$\therefore \frac{CC'}{K_m} = \frac{C'm}{K_o}$$

$$\therefore K_m = AC'$$

$$\therefore \frac{CC'}{AC'} = \frac{h/2}{R}$$

$$\therefore \epsilon_A = \frac{h/2}{R}$$

$$\therefore \epsilon'_A = \frac{y}{R} \rightarrow \textcircled{1}$$

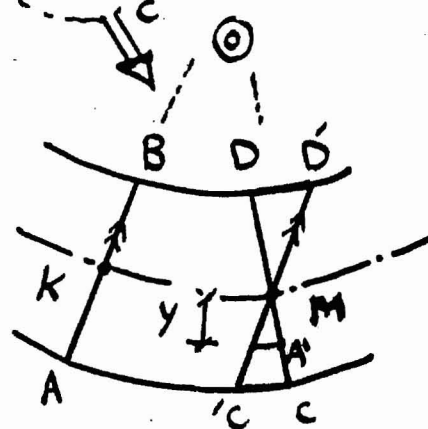
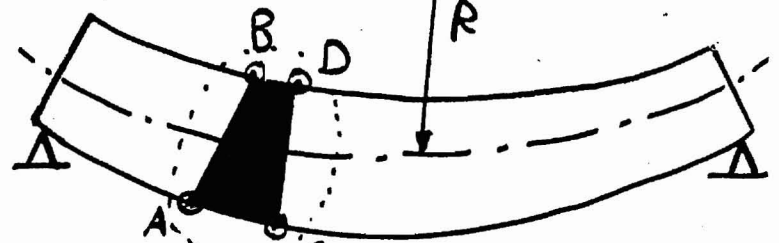
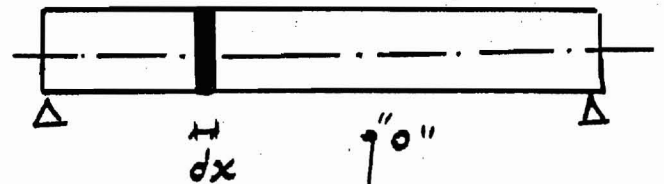
$$\therefore \epsilon'_A = B_t \cdot f_{A'}^n \rightarrow \textcircled{2}$$

From  $\textcircled{1}$ ,  $\textcircled{2}$  :

$$\therefore \frac{y}{R} = B_t \cdot f_{A'}^n$$

$$\therefore f_{A'} = \left( \frac{y}{R \cdot B_t} \right)^{1/n}$$

$$\therefore M = \int_{-\frac{h}{2}}^{\frac{h}{2}} f_{A'} \cdot b \cdot dy \cdot y$$



من شكل لحاب  
الزحف

$$M = \int_{-h/2}^{h/2} \sigma_A \cdot b \cdot dy \cdot y = \int_{-h/2}^{h/2} \left( \frac{y}{R \cdot B_t} \right)^{1/n} \cdot b \cdot dy \cdot y$$

$$= \frac{b}{(R B_t)^{1/n}} \int_{-h/2}^{h/2} y^{1+\frac{1}{n}} \cdot dy$$

$$= \frac{n \cdot b}{(2n+1)(R B_t)^{1/n}} \cdot \left[ y^{\frac{2n+1}{n}} \right]_{-h/2}^{h/2}$$

$$= \frac{2b}{\left(\frac{1}{n} + 2\right)(R \cdot B_t)^{1/n}} \cdot \left(\frac{h}{2}\right)^{\frac{1+2n}{n}}$$

$$\therefore M = \frac{(2b)^n}{B_t \cdot \left(\frac{1}{n} + 2\right)^n} \cdot \left(\frac{h}{2}\right)^{1+2n} \cdot \frac{1}{R}$$

$$\therefore \frac{M}{IE} = 1/R$$

$$\frac{M}{I} = \frac{\sigma}{y} = \frac{E}{R}$$

$$\therefore \frac{d^2 y}{dx^2} = -\frac{M}{EI}$$

hook  
منه لأض  
دو (أو) فنتقو

$$\therefore M^n = -D \cdot \frac{d^2 y}{dx^2}$$

hook  
ن علاقة بالزمن  
D : Const  
D =  $\frac{A \cdot \text{Const}}{t}$

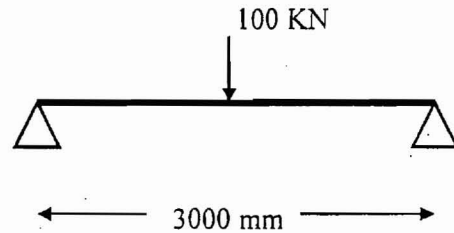
y : Deflection الزفيم

x : distance from support

و منه للتركيز

1- Simple beam (rectangular cross section with 120mm width and 200mm depth) subjected to concentrated load of 100kN as shown in fig (1).

Find the creep stress in beam and the total deformation at mid span after 10 years ( $K_4=8$ ,  $A=6.8 \times 10^{-23}$ )



1- Stress:

$$f_{cr} = f_e \cdot \left( \frac{2(K_4 + 1)}{K_4} \right)$$

$$\rightarrow f_e = \frac{M}{I} \cdot y$$

$$= \frac{P \cdot L}{4 \cdot \left( \frac{bh^3}{12} \right)} \cdot \frac{h}{2}$$

$$= \frac{(100 \times 1000 \times 3000)}{4 \left( \frac{120 \cdot (200)^3}{12} \right)} \cdot \frac{200}{2}$$

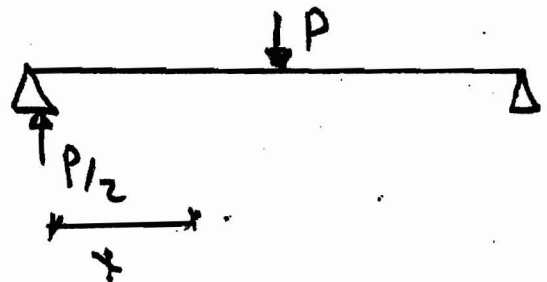
$$= 93.75 \text{ N/mm}^2 = \text{MPa}$$

$$\therefore f_{cr} = 93.75 \cdot \left( \frac{2 \cdot 8 + 1}{3 \cdot 8} \right) = \underline{\underline{66.4 \text{ MPa}}}$$

2. Deformation :

$$\frac{\partial^2 y}{\partial x^2} = \frac{t}{A} \cdot (M_x^{k_4})$$

$$\therefore \frac{\partial^2 y}{\partial x^2} = \frac{t}{A} \cdot \left(\frac{P}{2}x\right)^8$$



الحل :

$$\therefore \frac{\partial y}{\partial x} = \left(\frac{t}{A}\right) \int \frac{P^8}{(2)^8} x^8 \cdot dx$$

$$M_x = \frac{P}{2} \cdot x$$

(0 → L/2)

$$\frac{\partial y}{\partial x} = \frac{t}{A} \left(\frac{P^8}{2}\right) \cdot \frac{x^9}{9} + C_1 \rightarrow \textcircled{1}$$

الحل :  $y = \frac{t}{9A} \left(\frac{P}{2}\right)^8 \frac{x^{10}}{10} + C_1 x + C_2 \rightarrow \textcircled{2}$

الشروط :

$$\frac{\partial y}{\partial x} = 0.0 \rightarrow x_{\max} = L/2$$

$$\text{from } y = 0.0 \rightarrow x = 0.0$$

from  $\textcircled{2}$   $C_2 = 0.0$

$$\text{from } \textcircled{1} \quad C_1 = -\frac{t}{A} \left(\frac{P^8}{2}\right) \frac{(L/2)^9}{9}$$

$$\therefore y = \frac{t}{9A} \left(\frac{P}{2}\right)^8 \frac{x^{10}}{10} + \frac{-t}{A} \cdot \left(\frac{P}{2}\right)^8 \cdot \frac{(L/2)^9}{9}$$



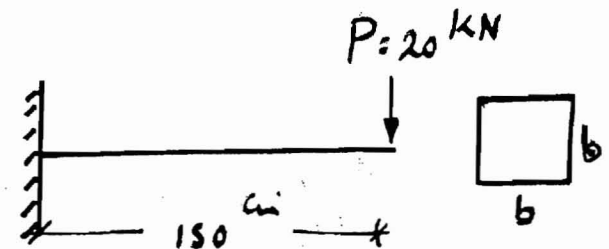
- 6) A cantilever beam of square cross section and length  $L = 150.0 \text{ cm}$  is subjected to an end concentrated load  $P = 20 \text{ kN}$ . Determine the cross sectional dimensions if a) the creep stress is not exceed  $80.0 \text{ MPa}$  and b) the creep deflection is to be less than  $1/50$  of the beam span in 10 years. Use the following equations:

$$\sigma = \sigma_{\text{elastic}} \left( \frac{2n+1}{3n} \right), \quad D = \left( \frac{1}{\beta_t} \right) \left[ \frac{(2b)^n \left( \frac{h}{2} \right)^{(2n+1)}}{(2 + 1/n)^n} \right], \text{ where } b = \text{width of beam, } h = \text{depth}$$

of beam,  $D \frac{d^2 y}{dx^2} = M^n$ ,  $n = 5$ , and  $\beta_t = 8 (10)^{-14} \text{ mm/mm per day}$ .

a)  $\therefore \frac{P}{A} = 80 \text{ MPa}$

$$\therefore \frac{P}{A} = \frac{P}{\text{elastic}} \cdot \left( \frac{2n+1}{3n} \right)$$



$$\therefore \frac{P}{\text{elastic}} = \frac{M}{I} \cdot y$$

$$= \frac{20 \cdot 150 \cdot 1000}{\frac{b \cdot b^3}{12}} \cdot \frac{b}{2} = \frac{18 \cdot 10^7}{b^3}$$

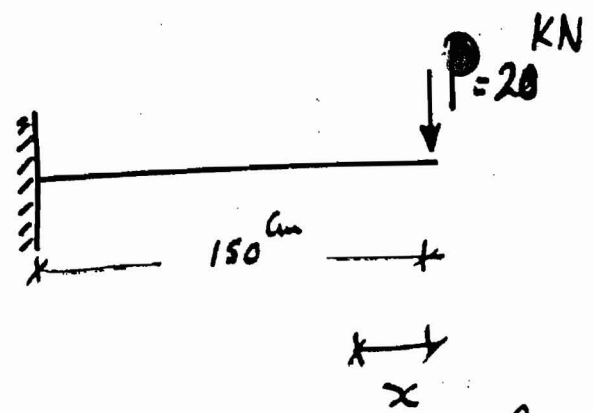
$$\frac{P}{A} = \frac{P}{\text{elastic}} \left( \frac{2n+1}{3n} \right)$$

$$\therefore 80 = \frac{18 \cdot 10^7}{b^3} \cdot \left( \frac{2 \cdot 5 + 1}{3 \cdot 5} \right)$$

$$\Rightarrow b = 118.2 \text{ mm}$$

$$= 11.8 \text{ cm}$$

أقصى انحراف  
b)  $y_{max} = \frac{1}{50} \cdot 150^5$   
 $= 3 \text{ cm}$



$$\therefore \frac{d^2 y}{dx^2} = \frac{1}{D} \cdot (M_x)''$$

$M_x = P \cdot x$

$$\therefore \frac{d^2 y}{dx^2} = \frac{1}{D} (Px)'' = \frac{1}{D} (P^5 \cdot x^5)$$

بالتكامل  
الأول  $\rightarrow \frac{dy}{dx} = \frac{P^5 \cdot x^6}{6 D} + C_1$

بالتكامل  
الأول  $\rightarrow y = \frac{P^5 \cdot x^7}{6 \cdot 7 \cdot D} + C_1 \cdot x + C_2$

Condition (1)  $\rightarrow \frac{dy}{dx} = \text{Zero} \text{ at } x = L$

دفع انحراف يمكن  
حاله في القاع الأول

$\therefore C_1 = -\frac{P^5 \cdot x^6}{6 D} = -\frac{P^5 \cdot L^6}{6 D} \rightarrow \textcircled{1}$

Condition (2)  $\rightarrow y = 0.0 \text{ at } x = L$

$$0.0 = \frac{P^5 \cdot L^7}{42 D} + \frac{-P^5 \cdot L^6 \cdot L}{6 D} + C_2$$

$$C_2 = \frac{P^5 \cdot L^7}{7 D} \rightarrow \textcircled{2}$$

$$\therefore y = \frac{P \cdot x^7}{42 D} - \frac{P \cdot L^6}{6 D} x + \frac{P \cdot L^7}{7 D}$$

$$\therefore y = y_{\max} \quad \text{at} \rightarrow x = 0.0$$

عند الطرف

$$\therefore y_{\max} = \frac{P \cdot L^7}{7 D}$$

$$y_{\max} = 3 \text{ cm} = 30 \text{ mm} = \frac{(20 \times 1000)^5 \cdot (1500)^7}{7 D}$$

Leqok

Constant  $\rightarrow D = 2.6 \cdot 10^{41}$

from relation :  $D = \frac{1}{B} \cdot \left[ \frac{(2b)^n \cdot \left(\frac{h}{2}\right)^{2n+1}}{\left(2 + \frac{1}{n}\right)^n} \right]$

$$\therefore 2.6 \cdot 10^{41} = \frac{1}{8 \cdot 10^{-14}} \cdot \left[ \frac{(2 \cdot b)^5 \cdot \left(\frac{b}{2}\right)^{2 \cdot 5 + 1}}{\left(2 + \frac{1}{5}\right)^5} \right]$$

$$\therefore b = 100.6 \text{ mm}$$

Use  $h = 110 \text{ cm}$

2- Design a vertical bar AB with length 2m subjected to 6 ton tensile load at 300° c after 10 years if :

1- Steel grade (24/36) and factor of safety = 4.

2- Allowable creep rate = 0.0012 at year.

Assume that the total instantaneous and primary elongation is 1.4 mm,  $f^o = 72 \text{ kg/cm}^2$ ,

$k_4 = 8$ ,  $k_3 = 5 \times 10^{-12} \text{ cm/cm/day}$

(1) Grade (24/36)

$$\therefore f_y = 24 \text{ kg/mm}^2$$

$$\therefore f_{all} = \frac{f_y}{F.O.S} = \frac{24}{4} = 6 \text{ kg/mm}^2$$

$$= 600 \text{ kg/cm}^2$$

$$\therefore f_{all} = \frac{P}{A}$$

$$\therefore Area = \frac{6000}{600}$$

$$= \underline{\underline{10 \text{ cm}^2}}$$

$$\therefore \underline{\underline{D = 3.57 \text{ cm}}}$$

(نوشتہ قال  $F.O.S$   
بکام ناظرہ  
 $F.O.S = 2$ )

$$2) \quad C = 0.0012 \quad \text{cm/cm/year}$$

$$C = K_3 \cdot \left( \frac{f}{f_0} \right)^{K_4}$$

$$f_0 = 72 \text{ Kg/cm}^2 \quad K_4 = 8$$

$$K_3 = 5 \times 10^{-12}$$

$$(0.0012 / 365) = 5 \times 10^{-12} \cdot \left( \frac{f}{72} \right)^8$$

$$f = 384.2 \text{ Kg/cm}^2$$

$$f = \frac{P}{A} = \frac{6000}{\text{Area}}$$

$$\text{Area} = \frac{6000}{384.2} = 15.6 \text{ cm}^2$$

$$D = 22.1 \text{ cm}$$

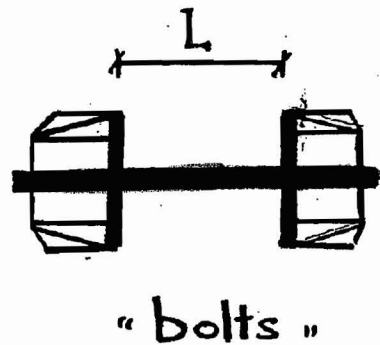
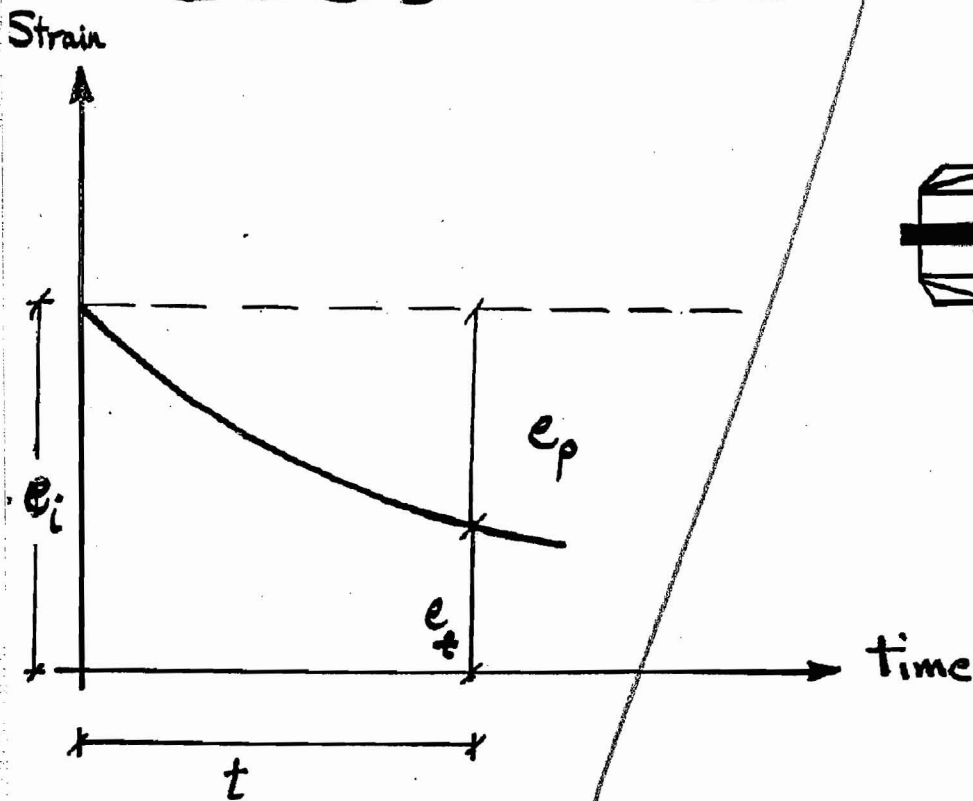
take D = 22.1 cm

# Stress Relaxation

## إجهاد الإسترخاء

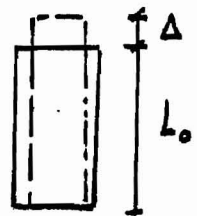
- عند ثبات الإرتعال يقل الإجهاد مع الزمن وتظهر

هذه الظاهرة من المسامير والزنسانة سابقته الإجهاد



→ After Loading :

$$e_i = \frac{f_i}{E}$$



→ After any time :

$$e_i = e_t + e_{creep}$$

$$\underline{e_i = e_t + e_p}$$

$e_i$  : initial strain      الإنفعال الابتدائي

$e_t$  : Strain at any time      الإنفعال عند أي زمن

$e_p$  : Creep Strain      إنفعال الزحف

$$(1) \quad \frac{f_i}{E} = \frac{f_t}{E} + \beta \cdot f_t^n \cdot t$$

$f_i$  : الإجهاد الابتدائي

$f_t$  : الإجهاد عند الزمن المطلوب

$$(2) \quad t = \frac{(f_0)^{k_4}}{E k_3 (k_4 - 1) f_t^{(k_4 - 1)}} \cdot \left( 1 - \left( \frac{f_t}{f_i} \right)^{k_4 - 1} \right)$$

يتم استخدام المعادلة على حسب العملية

- 4) A steel bolt is subjected to an axial tensile load fixed between two rigid plates so that the length of the bolt remains constant. What must be the initial stress to produce 65 percent of the initial stress after 10 years? Use the following equation:  $\frac{\sigma_i}{E} = \frac{\sigma}{E} + \beta \sigma^n$  and the constants  $n = 4$  &  $\beta = 4.6(10)^{-14}$  mm/mm/day and  $E = 200$  GPa.

$$f_t = 0.65 f_i \rightarrow 10 \text{ years}$$

$$\beta = 4.6 \cdot 10^{-14} \text{ mm/mm/day}, E = 200 \text{ GPa}$$

$$n = 4$$

sol

$$\frac{f_i}{E} = \frac{f_t}{E} + \beta \cdot t \cdot f_t^n$$

$$\therefore \frac{f_i}{200} = \frac{0.65 f_i}{200} + 4.6 \cdot 10^{-14}$$

$$\cdot 10 \cdot 365 \cdot (0.65 \cdot f_i)^4$$

$$\therefore f_i = 0.0391 \text{ GPa}$$

$$\therefore f_t = 0.025 \text{ GPa}$$



5) For the steel bolt in problem (4), estimate the time intervals to be retightened again for both initial stress calculated in problem (4) and for initial stress of 100 MPa if the decreasing of stress should not be less than half of initial stress. Comment on your results

$$f_i = 39.12 \text{ MPa}$$

$$f_t = 0.5 f_i$$

$$= 19.56 \text{ MPa}$$

$$\frac{f_i}{E} = \frac{f_t}{E} + B \cdot t \cdot f_t^n$$

$$\frac{39.12}{200 \cdot 10^3} = \frac{19.56}{200 \cdot 10^3} + 4.6 \cdot 10^{-14} \cdot t \cdot (0.5 \cdot 39.12)^4$$

$$\therefore t = 14525 \text{ day}$$

$$f_i = 100 \text{ MPa}$$

$$f_t = 0.5 f_i$$

$$= 50 \text{ MPa}$$

$$\frac{f_i}{E} = \frac{f_t}{E} + B \cdot t \cdot f_t^n$$

$$\frac{100}{200 \cdot 10^3} = \frac{50}{200 \cdot 10^3} + 4.6 \cdot 10^{-14} \cdot t \cdot (50)^4$$

$$t = 869 \text{ day}$$

← بزيادة الإجهاد الابتدائي يزداد معدل الاسترخاء

وقت الزمن اللازم

لفك

وسام

Look

6. A steel bolt is subjected to an axial tensile load fixed between two rigid plates so that the length of the bolt remains constants. What must be the initial stress to produce 75 % of the initial stress after 3 years?

The constants:  $P = 72 \text{ kg/cm}^2$ ,  $k_4 = 8$ ,  $k_3 = 5 \times 10^{-10} \text{ cm/cm/day}$ ,  $E = 2 \times 10^6 \text{ kg/cm}^2$

Sol

$$t = \frac{(P_0)^{k_4}}{E k_3 (k_4 - 1) P_f^{(k_4 - 1)}} \cdot \left(1 - \left(\frac{P_f}{P_i}\right)^{(k_4 - 1)}\right)$$

$$\therefore \frac{P_f}{P_i} = \frac{75}{100} = 0.75$$

$$\therefore 3 \times 365 = \frac{(72)^8}{2 \times 10^6 \times 5 \times 10^{-10} (8 - 1) \cdot P_f^{(8 - 1)}} \left(1 - (0.75)^{(8 - 1)}\right)$$

حل المعادلة

$$\therefore P_f = 97.2 \text{ kg/cm}^2$$

الاجواب بعد زمن 3 سنوات (موجود على هيئة)

الاجابة

(18)